

# Relaciones trigonométricas

$$\operatorname{sen} \alpha = \frac{y}{r}$$

$$\cos \alpha = \frac{x}{r}$$

$$\operatorname{tg} \alpha = \frac{y}{x}$$

$$\operatorname{ctg} \alpha = \frac{x}{y}$$

$$\operatorname{cos ec} \alpha = \frac{r}{y}$$

$$\sec \alpha = \frac{r}{x}$$

$$\operatorname{tg} \alpha = \frac{\operatorname{sen} \alpha}{\cos \alpha}$$

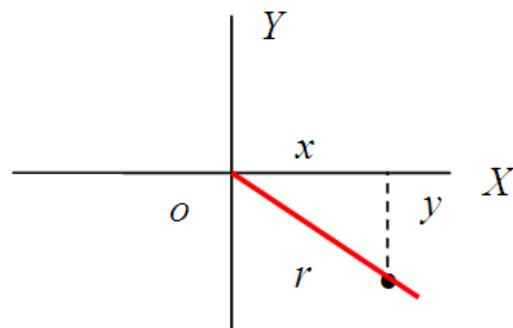
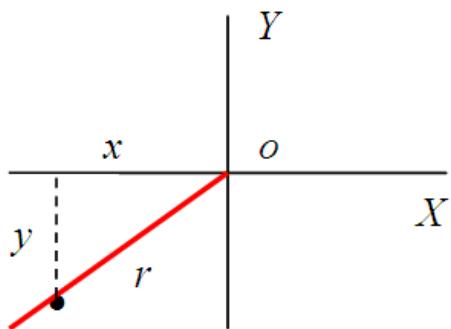
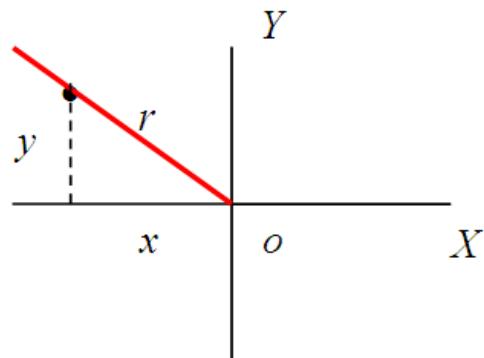
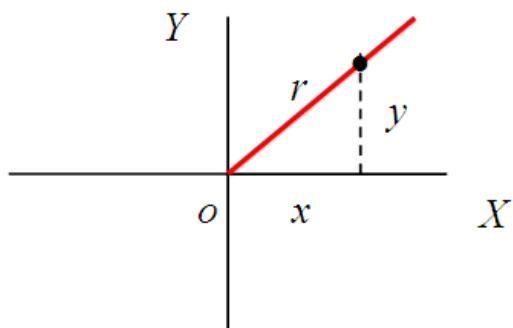


Fig. Graficas de las Funciones Trigonometricas

# Identidades trigonométricas

$$\operatorname{sen} (\alpha \pm \beta) = \operatorname{sen} \alpha \cos \beta \pm \cos \alpha \operatorname{sen} \beta$$

$$\cos (\alpha \pm \beta) = \cos \alpha \cos \beta \mp \operatorname{sen} \alpha \operatorname{sen} \beta$$

$$\operatorname{sen} \alpha \pm \operatorname{sen} \beta = 2 \operatorname{sen} \frac{1}{2}(\alpha \pm \beta) \cos \frac{1}{2}(\alpha \mp \beta)$$

$$\cos \alpha + \cos \beta = 2 \cos \frac{1}{2}(\alpha + \beta) \cos \frac{1}{2}(\alpha - \beta)$$

$$\cos \alpha - \cos \beta = -2 \operatorname{sen} \frac{1}{2}(\alpha + \beta) \operatorname{sen} \frac{1}{2}(\alpha - \beta)$$

$$\operatorname{sen} \alpha \operatorname{sen} \beta = \frac{1}{2} [\cos (\alpha - \beta) - \cos (\alpha + \beta)]$$

$$\cos \alpha \cos \beta = \frac{1}{2} [\cos (\alpha - \beta) + \cos (\alpha + \beta)]$$

$$\operatorname{sen} \alpha \cos \beta = \frac{1}{2} [\operatorname{sen} (\alpha - \beta) + \operatorname{sen} (\alpha + \beta)]$$

$$\operatorname{sen} 2\alpha = 2 \operatorname{sen} \alpha \cos \alpha$$

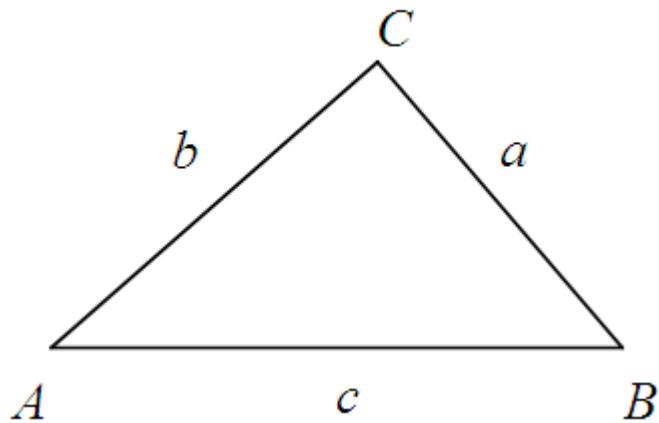
$$\cos 2\alpha = \cos^2 \alpha - \operatorname{sen}^2 \alpha$$

$$\cos^2 \frac{1}{2}\alpha = \frac{1}{2}(1 + \cos \alpha)$$

$$\operatorname{sen}^2 \frac{1}{2}\alpha = \frac{1}{2}(1 - \cos \alpha)$$

### Ley de los senos

$$\frac{a}{\operatorname{sen} A} = \frac{b}{\operatorname{sen} B} = \frac{c}{\operatorname{sen} C}$$



### Ley de los cosenos

$$a^2 = b^2 + c^2 - 2bc \cos A$$