

Formulario ¹	$m_m = \sum_{i=1}^N m_i$	$n_m = \sum_{i=1}^N n_i$	$m_i = n_i M_i$	$M_m = \frac{m_m}{n_m}$
$y_i = \frac{n_i}{n_m}$	$\sum_{i=1}^N y_i = 1$	$g_i = m f_i = \frac{m_i}{m_m}$	$\sum_{i=1}^N g_i = 1$	$R_m = \frac{R}{M_m}$
$y_i = \frac{\%V_i}{100}$	$M_m = \sum_{i=1}^N y_i M_i$	$g_i = y_i \frac{M_i}{M_m}$	$\%m_i = 100g_i$	$R_m = \frac{1}{\sum_{i=1}^N \frac{y_i}{R_i}}$
$g_i = \frac{\%m_i}{100}$	$M_m = \frac{1}{\sum_{i=1}^N \frac{g_i}{M_i}}$	$y_i = g_i \frac{M_m}{M_i}$	$\%V_i = 100y_i$	$R_m = \sum g_i R_i$

Dalton: $P_m = \sum_{i=1}^N P_i$ $y_i = \frac{P_i}{P_m}$ **Amagat:** $V_m = \sum_{i=1}^N V_i$ $y_i = \frac{V_i}{V_m}$ $T_i = T_m$ para ambos modelos

$U_m = n_m \bar{u}_m = \sum_{i=1}^N n_i \bar{u}_i = m_m u_m = \sum_{i=1}^N m_i u_i$ $\bar{u}_m = \sum_{i=1}^N y_i \bar{u}_i$ $u_m = \sum_{i=1}^N g_i u_i$

$\bar{C}_{v0}$ variable: $\begin{cases} \bar{u}_i(T) : \text{valor leído en las Tablas A-12 a A-19} \\ \bar{u}_i(T) = 100 \int_{\theta_{ref}}^{\theta} \bar{C}_{p0,i}(\theta) d\theta - \bar{R}T \text{ (Tabla A-9) (hidrocarburos)} \\ \bar{u}_i(T) = C_{v0,i} M_i (T - T_{ref}) \text{ (Tabla A-8) (gases monoatómicos)} \end{cases}$

$\bar{C}_{v0}$ constante: $\bar{u}_m = \bar{C}_{v0m} T_m$ $\bar{C}_{v0m} = \sum_{i=1}^N y_i \bar{C}_{v0,i} = \sum_{i=1}^N y_i C_{v0,i} M_i$ (Tabla A-8) (todos los gases)

$H_m = n_m \bar{h}_m = \sum_{i=1}^N n_i \bar{h}_i = m_m h_m = \sum_{i=1}^N m_i h_i$ $\bar{h}_m = \sum_{i=1}^N y_i \bar{h}_i$ $h_m = \sum_{i=1}^N g_i h_i$

$\bar{C}_{p0}$ variable: $\begin{cases} \bar{h}_i(T) : \text{valor leído en las Tablas A-12 a A-19} \\ \bar{h}_i(T) = 100 \int_{\theta_{ref}}^{\theta} \bar{C}_{p0,i}(\theta) d\theta \text{ (Tabla A-9) (hidrocarburos)} \\ \bar{h}_i(T) = C_{p0,i} M_i (T - T_{ref}) \text{ (Tabla A-8) (gases monoatómicos)} \end{cases}$

$\bar{C}_{p0}$ constante: $\bar{h}_m = \bar{C}_{p0m} T_m$ $\bar{C}_{p0m} = \sum_{i=1}^N y_i \bar{C}_{p0,i} = \sum_{i=1}^N y_i C_{p0,i} M_i$ (Tabla A-8) (todos los gases)

Si C_{v0} y C_{p0m} se consideran constantes: $C_{v0m} = \sum_{i=1}^N g_i C_{v0,i}$ $C_{p0m} = \sum_{i=1}^N g_i C_{p0,i}$

$\Delta S_m = \sum_{i=1}^N n_i \Delta \bar{s}_i$ $\Delta \bar{s}_i = \bar{s}_i(T_{m2}, P_{m2}) - \bar{s}_i(T_{m1}, P_{m1}) = \bar{s}_{i,2}^0 - \bar{s}_{i,1}^0 - \bar{R} \ln \frac{P_{m2} y_{i,2}}{P_{m1} y_{i,1}}$

$S_m = \sum_{i=1}^N n_i \bar{s}_i(T_m, P_m)$ $\bar{s}_i(T_m, P_m) = \bar{s}_i^0(T_m) - \bar{s}_i^0(T_{ref}) - \bar{R} \ln \frac{P_m y_i}{P_{ref}}$

$\bar{C}_{p0}$ variable: $\begin{cases} \bar{s}_i^0(T_m) : \text{valor leído en las Tablas A-12 a A-19} \\ \bar{s}_i^0(T_m) = \int_{\theta_{ref}}^{\theta_{T_m}} \frac{\bar{C}_{p0,i}(\theta)}{\theta} d\theta \text{ (Tabla A-9) (hidrocarburos)} \\ \bar{s}_i^0(T_m) = C_{p0,i} M_i \ln \left(\frac{T_m}{T_{ref}} \right) \text{ (Tabla A-8) (gases monoatómicos)} \end{cases}$

$\bar{C}_{p0}$ constante: $\bar{s}_i^0(T_m) = C_{p0,i} M_i \ln \left(\frac{T_m}{T_{ref}} \right)$ (Tabla A-8) (todos los gases)

GAS REAL $P_m V_m = Z_m m_m R_m T_m$ $P_m v_m = Z_m R_m T_m$ $P_m \bar{v}_m = Z_m \bar{R} T_m$

Regla de Kay $Z_m = Z(P_{r,m}, T_{r,m})$ $P_{c,m} = \sum_{i=1}^N y_i P_{c,i}$ $P_{r,m} = \frac{P_m}{P_{c,m}}$ $T_{c,m} = \sum_{i=1}^N y_i T_{c,i}$ $T_{r,m} = \frac{T_m}{T_{c,m}}$

$v_{r,i,m} = \frac{V_m P_{c,m}}{n_m \bar{R} T_{c,m}}$ **Tablas:** $H_m = \sum n_i \bar{h}_i^* - n_m D \bar{h}_m \bar{R} T_{c,m}$ $U_m = H_m - P_m V_m$ $S_m = \sum n_i \bar{s}_i^* - n_m D \bar{s}_m \bar{R}$

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Repaso Termodinámica I

$$\frac{T_2}{T_1} = \left(\frac{P_2}{P_1}\right)^{\frac{n-1}{n}} = \left(\frac{v_1}{v_2}\right)^{n-1}$$

$$C_p - C_v = R$$

$$k = \frac{C_p}{C_v}$$

$$k_m = \frac{C_{p,m}}{C_{v,m}}$$

$$\delta w_{rev} = P dv$$

$$\delta q_{rev} = T ds$$

$$(\delta q - \delta w = du)_{sistema}$$

$$W_{(n=1)} = mRT \ln \left(\frac{P_1}{P_2}\right)$$

$$W_{(n \neq 1)} = \frac{P_2 V_2 - P_1 V_1}{1 - n} = mR \frac{T_2 - T_1}{1 - n}$$

Mezclas Reales de Gases: Proceso de Llenado

Asumiendo que se tiene un tanque en el cual es posible cualquier tipo de interacción mecánica (W) y térmica (Q).

Supóngase también que los componentes involucrados en el proceso se dividen en:

- A) Componentes que inicialmente están en el tanque y también en la línea de llenado.
- B) Componentes que inicialmente solo están en el tanque.
- C) Componentes que inicialmente solo están en la línea de llenado.

Ecuaciones de continuidad: $\boxed{\sum n_{e,A} = \sum n_{2,A} - \sum n_{1,A}}$, $\boxed{\sum n_{2,B} = \sum n_{1,B}}$ y $\boxed{\sum n_{2,C} = \sum n_{e,C}}$

Primera Ley de la Termodinámica:

$$Q_{1 \rightarrow 2} - W_{1 \rightarrow 2} = \sum n_{2,A} (\bar{h}_{2,A} - \bar{h}_{e,A}) - \sum n_{1,A} (\bar{h}_{1,A} - \bar{h}_{e,A}) + \quad (1a)$$

$$\sum n_{2,C} (\bar{h}_{2,C} - \bar{h}_{e,C}) + \sum n_{1,B} (\bar{h}_{2,B} - \bar{h}_{1,B}) - \quad (1b)$$

$$\bar{R} (n_2 D \bar{h}_2 T_{c,2} - n_1 D \bar{h}_1 T_{c,1} - n_e D \bar{h}_e T_{c,e}) - \quad (1c)$$

$$(P_2 V_2 - P_1 V_1) \quad (1d)$$

Donde: $\bar{h}_b - \bar{h}_a = \begin{cases} MCp_o (T_b - T_a) & Cp_o \text{ constante, Tabla A-8} \\ M (h_b - h_a) & \text{Tabla A-10} \\ \bar{h}_b - \bar{h}_a & \text{Tablas A-12} \rightarrow \text{A-19} \\ 100 \int_{\theta_a}^{\theta_b} \bar{C}p_o(\theta) d\theta & \text{Tabla A-9} \end{cases}$

Segunda Ley de la Termodinámica:

$$\Delta S_U = \sum n_{2,A} (\bar{s}_{2,A} - \bar{s}_{e,A}) - \sum n_{1,A} (\bar{s}_{1,A} - \bar{s}_{e,A}) + \quad (2)$$

$$\sum n_{2,C} (\bar{s}_{2,C} - \bar{s}_{e,C}) + \sum n_{1,B} (\bar{s}_{2,B} - \bar{s}_{1,B}) - \quad (3)$$

$$\bar{R} (n_2 D \bar{s}_2 - n_1 D \bar{s}_1 - n_e D \bar{s}_e) - \frac{Q_{vc}}{T_o} \quad (4)$$

Donde:

$$\bar{s}_b - \bar{s}_a = \begin{cases} MCp_o \ln \left(\frac{T_b}{T_a}\right) - \bar{R} \ln \left(\frac{P_{m,b} y_b}{P_{m,a} y_a}\right) & Cp_o \text{ constante, Tabla A-8} \\ M (s_b^o - s_a^o) - \bar{R} \ln \left(\frac{P_{m,b} y_b}{P_{m,a} y_a}\right) & \text{Tabla A-10} \\ \bar{s}_b^o - \bar{s}_a^o - \bar{R} \ln \left(\frac{P_{m,b} y_b}{P_{m,a} y_a}\right) & \text{Tablas A-12} \rightarrow \text{A-19} \\ \int_{\theta_a}^{\theta_b} \frac{\bar{C}p_o(\theta)}{\theta} d\theta - \bar{R} \ln \left(\frac{P_{m,b} y_b}{P_{m,a} y_a}\right) & \text{Tabla A-9} \end{cases} \quad (5)$$